# Deep Learning for Computer Vision

Fall 2022

https://cool.ntu.edu.tw/courses/189345 (NTU COOL)

http://vllab.ee.ntu.edu.tw/dlcv.html (Public website)

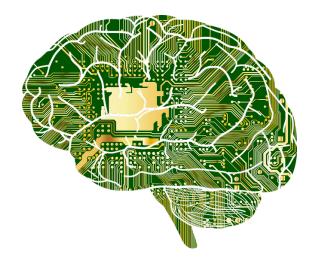
Yu-Chiang Frank Wang 王鈺強, Professor Dept. Electrical Engineering, National Taiwan University

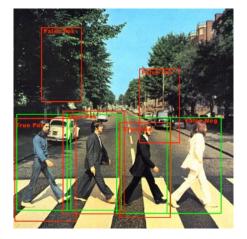
2022/09/27

#### What's to Be Covered Today...

- Segmentation
- Object Detection
- Generative Model
- HW #1 is out & due Oct. 10<sup>th</sup> Mon 23:59







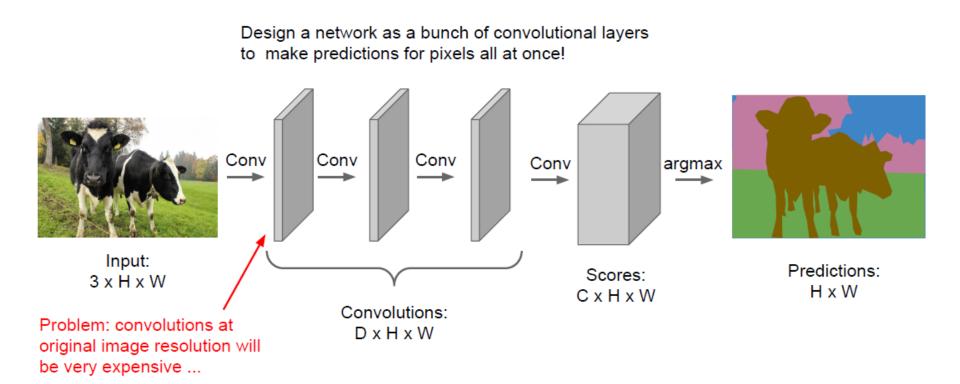
#### A Practical Segmentation Task

- Semantic Segmentation
  - Supervised learning
  - Assign a class label to each pixel in the input image (i.e., pixel-level classification)
  - Not like instance segmentation, do not differentiate instances; only care about pixel labels



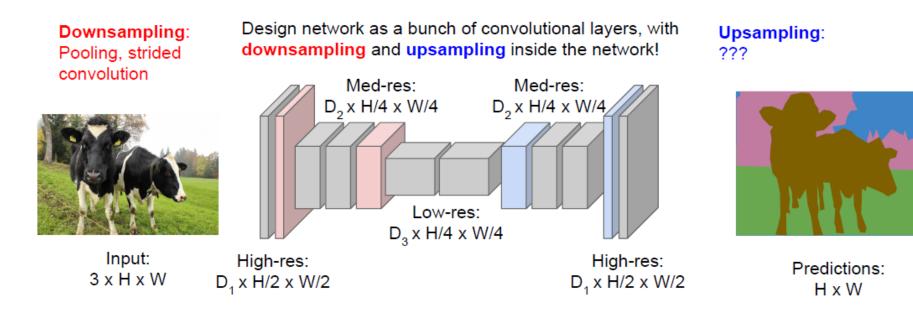
# **Semantic Segmentation**

• Fully Convolutional Nets



# **Semantic Segmentation**

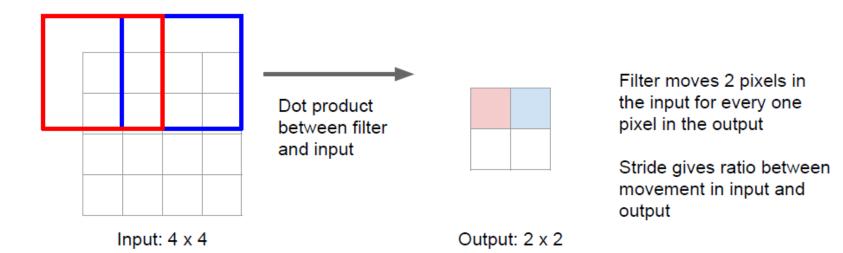
• Fully Convolutional Nets (cont'd)



Long, Shelhamer, and Darrell, "Fully Convolutional Networks for Semantic Segmentation", CVPR 2015 Noh et al, "Learning Deconvolution Network for Semantic Segmentation", ICCV 2015

# **In-Network Downsampling**

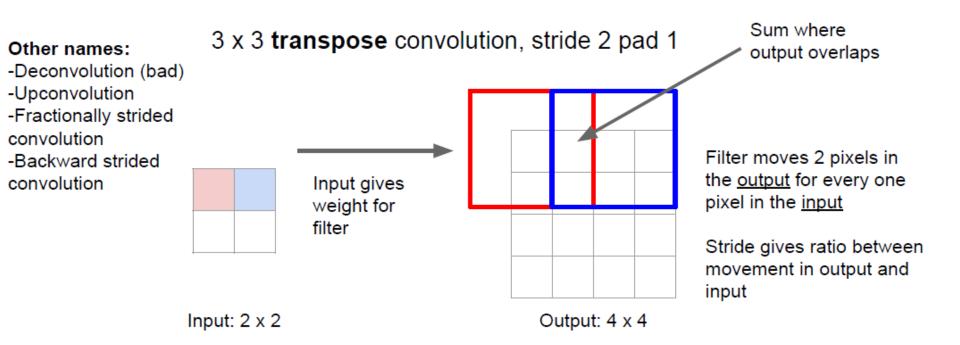
• Revisit: Learnable Downsampling: Convolution



Recall: Normal 3 x 3 convolution, stride 2 pad 1

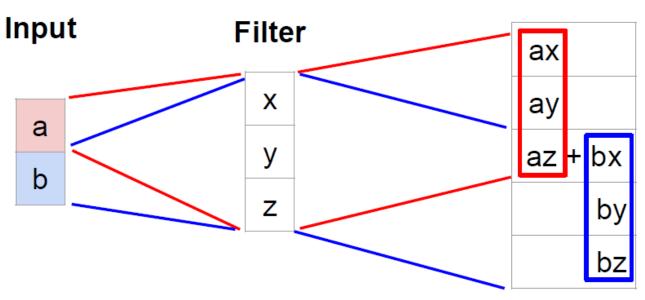
# **In-Network Upsampling**

• Transpose Convolution



# **In-Network Upsampling**

- Transpose Convolution
  - 1D example



Output

Output contains copies of the filter weighted by the input, summing at where at overlaps in the output

Need to crop one pixel from output to make output exactly 2x input

#### **In-Network Upsampling**

- Transpose Convolution
  - Example as matrix multiplication

We can express convolution in terms of a matrix multiplication

$$\vec{x} * \vec{a} = X\vec{a}$$

$$\begin{bmatrix} x & y & x & 0 & 0 & 0 \\ 0 & x & y & x & 0 & 0 \\ 0 & 0 & x & y & x & 0 \\ 0 & 0 & 0 & x & y & x \end{bmatrix} \begin{bmatrix} 0 \\ a \\ b \\ c \\ d \\ 0 \end{bmatrix} = \begin{bmatrix} ay + bz \\ ax + by + cz \\ bx + cy + dz \\ cx + dy \end{bmatrix}$$

Example: 1D conv, kernel size=3, stride=1, padding=1

Convolution transpose multiplies by the transpose of the same matrix:

$$\vec{x} *^T \vec{a} = X^T \vec{a}$$

 $\begin{bmatrix} x & 0 & 0 & 0 \\ y & x & 0 & 0 \\ z & y & x & 0 \\ 0 & z & y & x \\ 0 & 0 & z & y \\ 0 & 0 & 0 & z \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} ax \\ ay + bx \\ az + by + cx \\ bz + cy + dx \\ cz + dy \\ dz \end{bmatrix}$ 

When stride=1, convolution transpose is just a regular convolution (with different padding rules)

Remarks

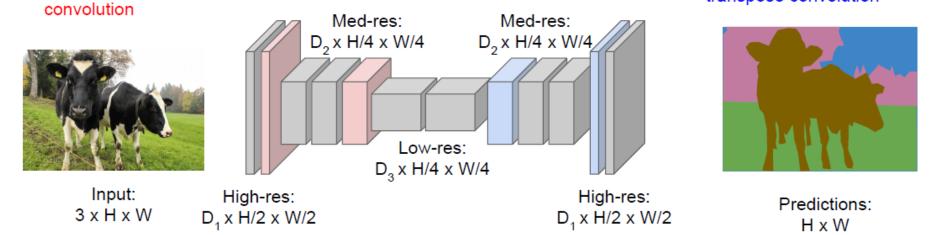
Downsampling:

Pooling, strided

- All layers are convolutional
- End-to-end training

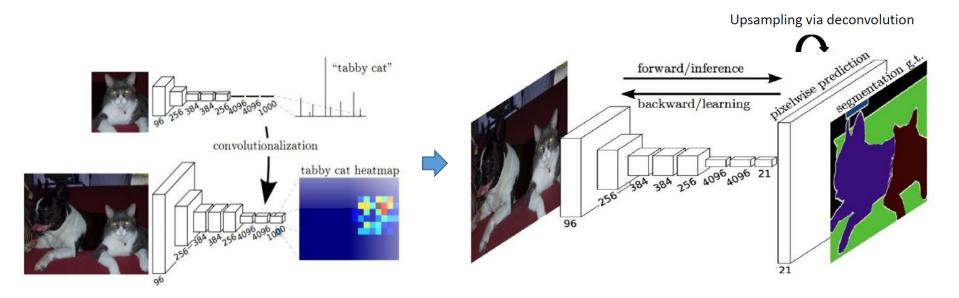
Design network as a bunch of convolutional layers, with downsampling and upsampling inside the network!

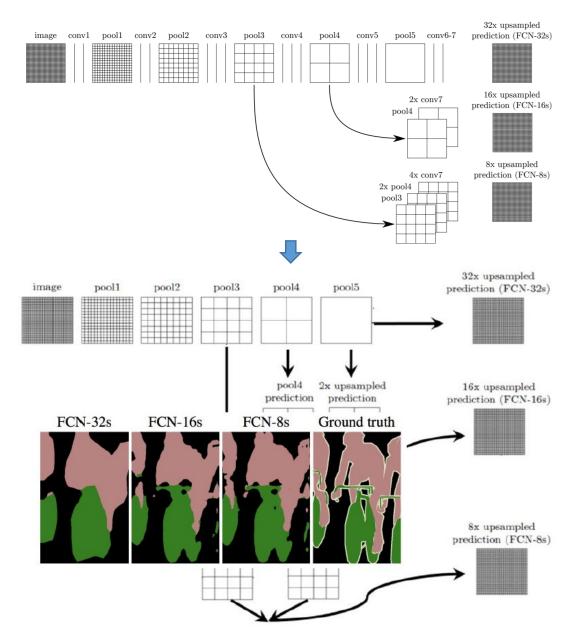
**Upsampling**: Unpooling or strided transpose convolution



Long, Shelhamer, and Darrell, "Fully Convolutional Networks for Semantic Segmentation", CVPR 2015 Noh et al, "Learning Deconvolution Network for Semantic Segmentation", ICCV 2015

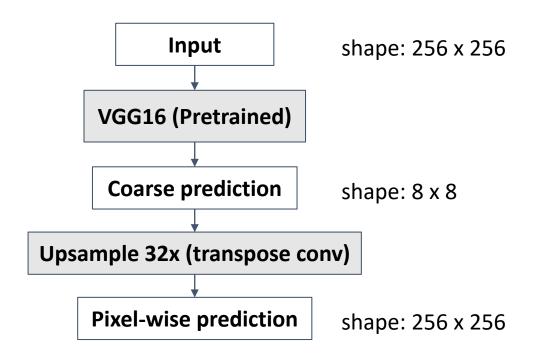
- More details
  - Use transpose convolution to upsample pixel-wise classification results
  - Adapt existing classification network to fully convolutional forms
  - Remove flatten layer and replace fully connected layers with conv layers
  - Append 1 x 1 conv layer with channel dims to predict scores for each class





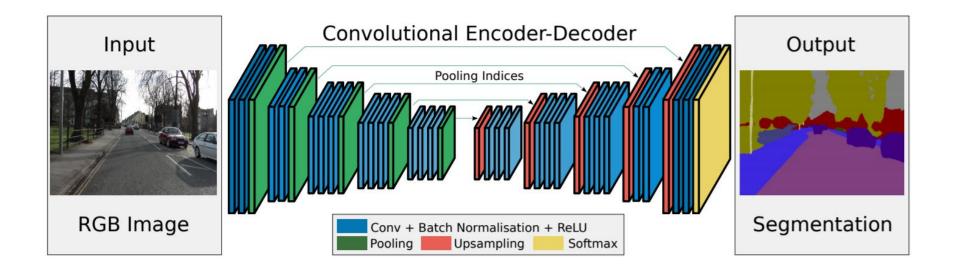
- Example
  - VGG16-FCN32s
  - Loss: pixel-wise cross-entropy

i.e., compute cross-entropy between each pixel and its label, and average over all of them



# SegNet

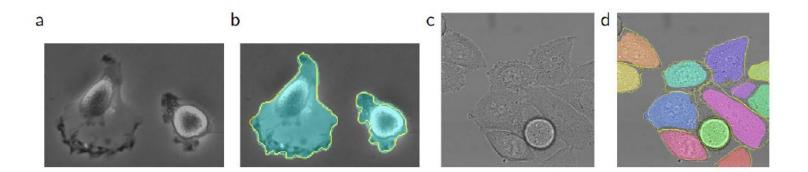
- Efficient architecture (memory + computation time)
- Upsampling reusing max-unpooling indices
- Reasonable results without performance boosting addition
- Comparable to FCN



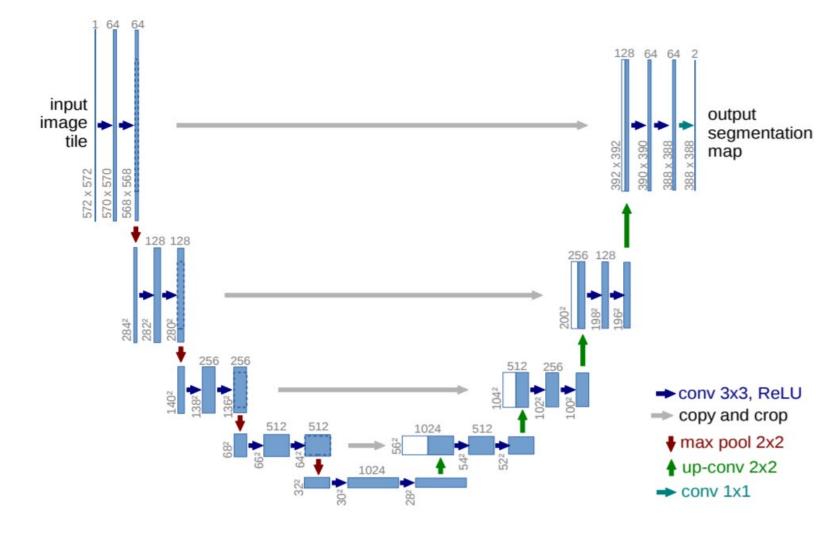
"SegNet: A Deep Convolutional Encoder-Decoder Architecture for Image Segmentation" [link]

#### **U-Net** (Ronneberger et al., MICCAI'15)

- Remarks
  - In biomedical image segmentation, localization is critical; in other words, precise semantic segmentation is desirable
  - Plus, # of training images might not be sufficient.



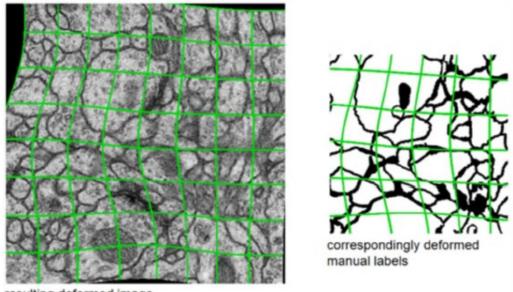
#### U-Net (cont'd)



U-Net: Convolutional Networks for Biomedical Image Segmentation [link]

#### Additional Remarks: Elastic Deformation for Pre-processing

- Data augmentation is crucial for U-Net (and more DL models)
- Elastic deformation allows manipulation of medical images & GT seg maps



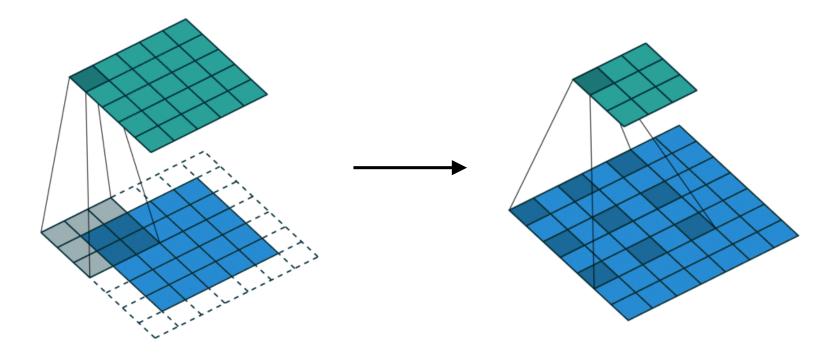
resulting deformed image (for visualization: no rotation, no shift, no extrapolation)

#### Additional Remarks: Enhanced Spatial Information

- For semantic segmentation, spatial information is of great importance
- It is desirable for the model to observe
  - Both the target pixel and its **neighboring areas** 
    - Recall: Atrous (or dilated) convolution
  - Features across **different scales** should be considered
    - Spatial Pyramid Pooling

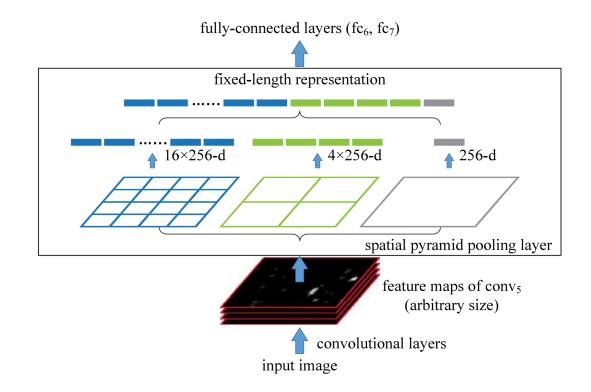
## **Revisit of Dilated Convolution**

- Atrous (Dilated) Convolution
  - Larger receptive field with the same kernel size (e.g., a 3x3 kernel depicted below with different receptive field)



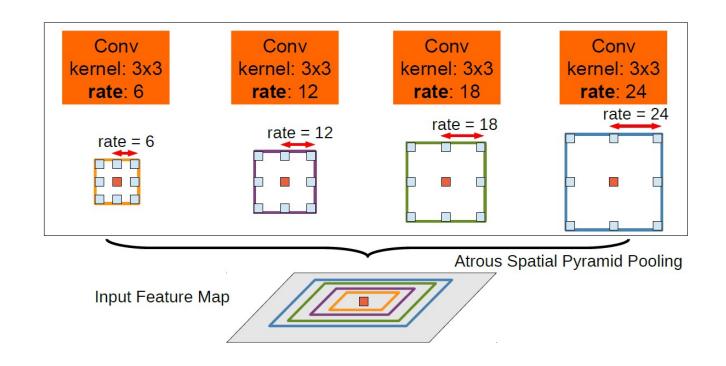
#### **Spatial Pyramid Pooling (SPM)**

- Goal:
  - Integrating information viewed under different scales



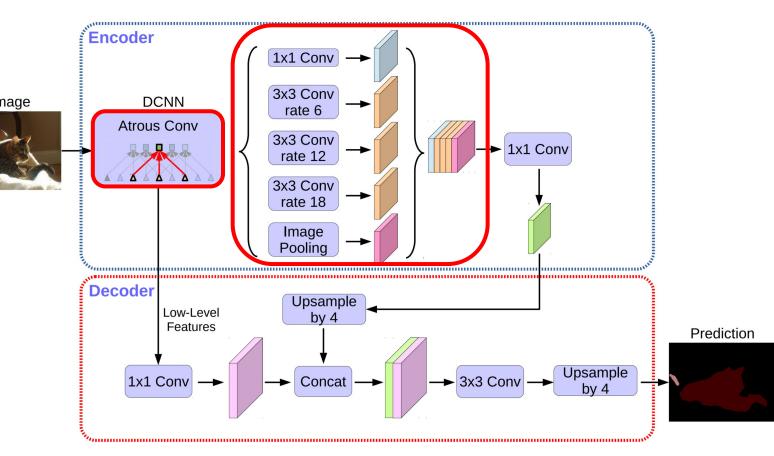
#### Thus, we have...

- Atrous Spatial Pyramid Pooling
  - Combines both techniques for producing enhanced spatial info



#### DeepLabv3+

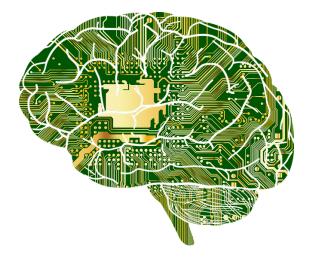
Image



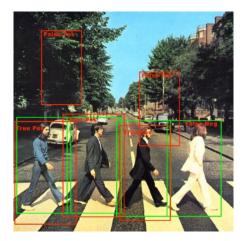
Chen et al. "Encoder-decoder with atrous separable convolution for semantic image segmentation," ECCV 2018

#### What's to Be Covered Today...

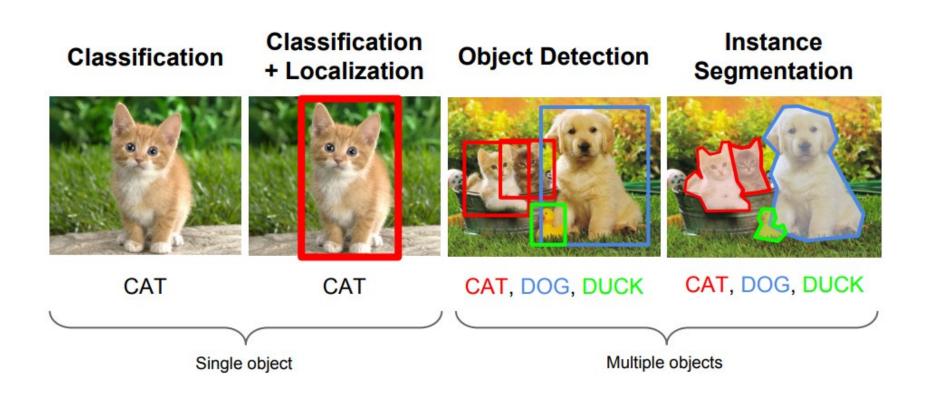
- Segmentation
- Object Detection
- Generative Model





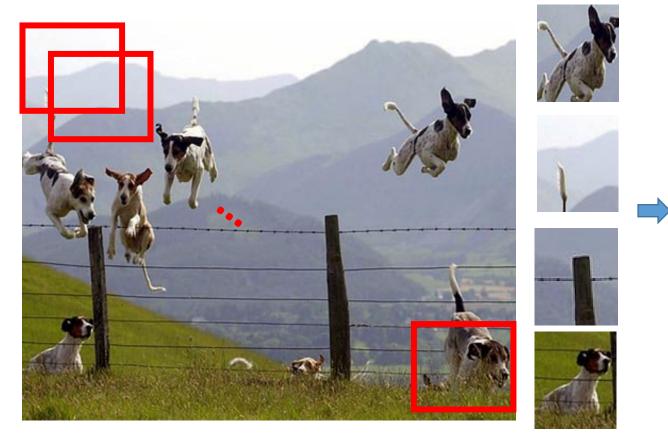


# Roadmap



# **Object Category Detection**

- Focus on object search: "Where is it?"
- Build templates that quickly differentiate object patch from background patch

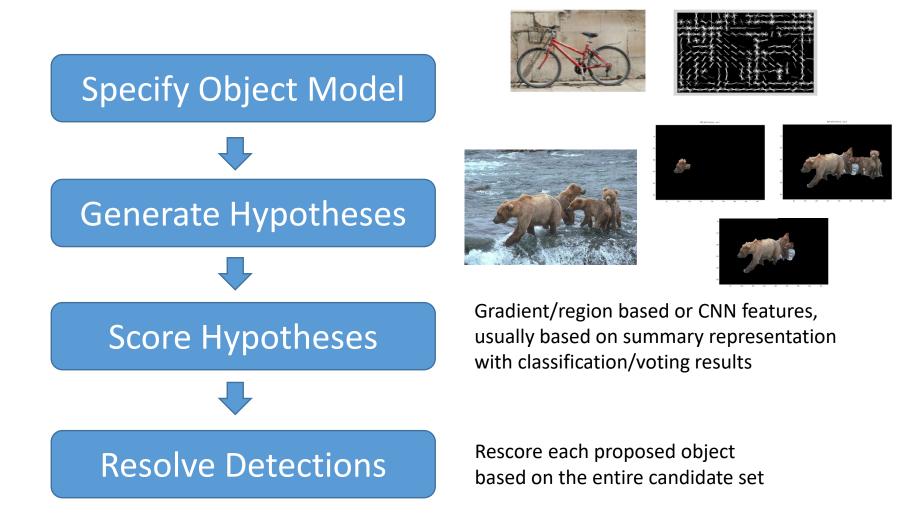


Dog Model



Object or Non-Object?

## **General Process of Object Recognition**



## **Challenges in Modeling the Object Classes**





#### Object pose



Clutter



Occlusion



Intra-class appearance



Viewpoint

# **Challenges in Modeling the Non-object Classes**

True Detection



Bad Localization



Confused with Similar Object





Misc. Background





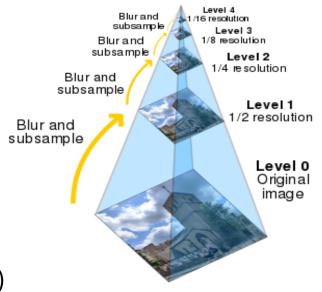


Confused with Dissimilar Objects



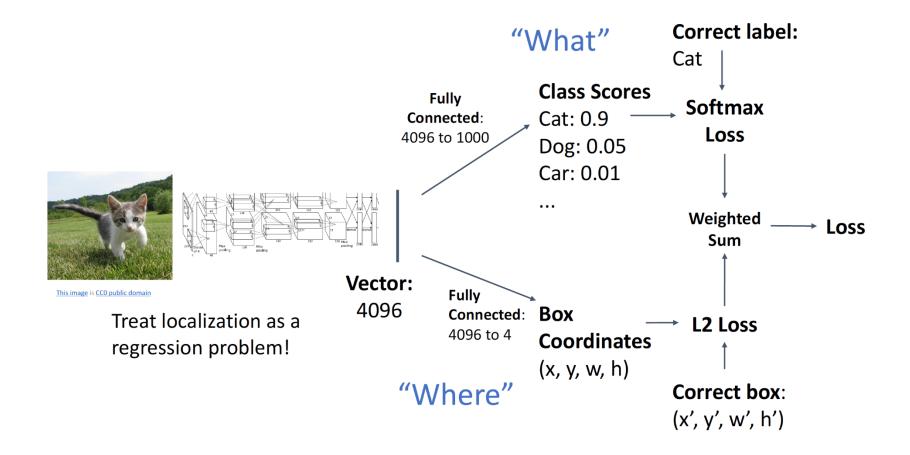
# **Type of Approaches**

- Sliding Windows
  - "Slide" a box around the input image
  - Classify each cropped image region inside the box and determine if it's an object of interest or not
  - E.g., HOG (person) detector by Dalal and Triggs (2005) Deformable part-based model by Felzenswalb et al. (2010) Real-time (face) detector by Viola and Jones (2001)
- Region (Object) Proposals
  - Generate region (object) proposals
  - Classify each image region and determine it's an object or not



#### Type of Approaches (cont'd)

• CNN-based Methods



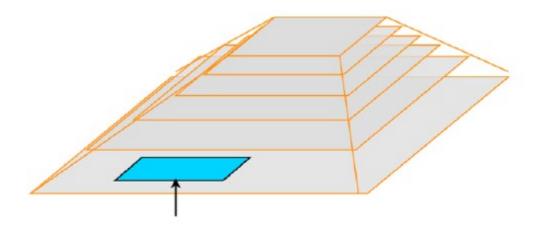
#### **Before the Rise/Resurgence of CNN:** The HOG Detector

- Histogram of Oriented Gradients
- Sliding window detector find objects in 4 steps:
  - Inspect every window ٠
  - Extract features in window ٠
  - Classify & accept window if score > threshold •
  - Clean-up (post-processing) stage ٠

**Detection window** 



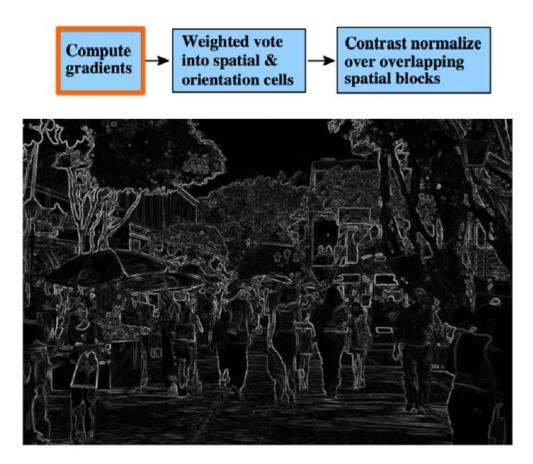
- Step 1: Inspect every window
  - Objects can vary in sizes, what to do?
  - Sliding window + image pyramid!



#### Scale-space pyramid

**Detection window** 

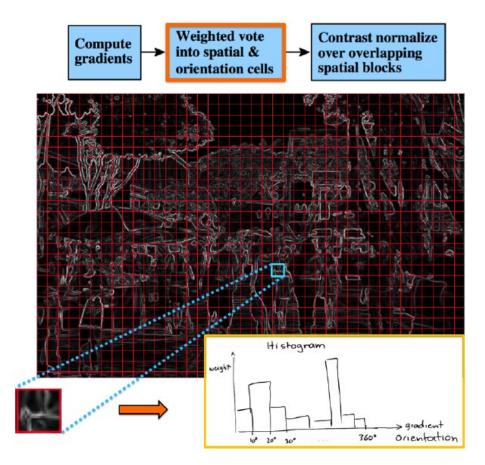
- Step 2: Extract Features in Window
  - Histogram of Oriented Gradients (HOG) features
  - Similar to SIFT in some ways...
    - ever heard of SIFT?



- Step 2: Extract Features in Window
  - Histogram of Gradients (HOG) features
  - Ways to compute image gradients...

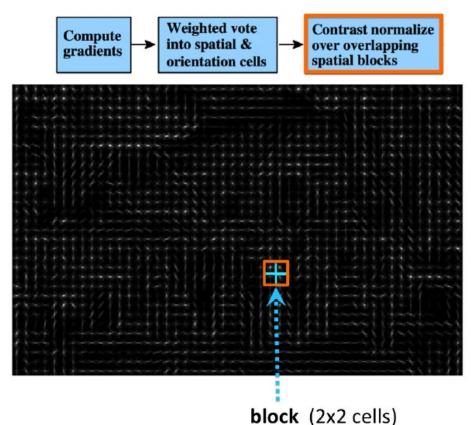
| Mask<br>Type                                    | 1D<br>centered | 1D<br>uncentered | 1D<br>cubic-corrected | 2x2 diagonal  | 3x3 Sobel   |
|---|----------------|------------------|-----------------------|---|---|
| Operator  | [-1, 0, 1]     | [-1, 1]          | [1, -8, 0, 8, -1]     | $\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$ $\begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$ | $\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$ $\begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$ |
| Miss rate<br>at 10 <sup>-4</sup><br>FPPW        | 11%            | 12.5%            | 12%                   | 12.5%   | 14%   |
| (Miss rate: smaller is better,                  |                |                  |                       |   |   |
| This gradient filter gives the best performance |                |                  |                       |   |   |

- Step 2: Extract Features in Window
  - Histogram of Gradients (HOG) features
  - Divide the image into non-overlapping cells (grids) of 8 x 8 pixels
  - Compute a histogram of orientations in each cell, resulting in a 9-dimensional feature vector.

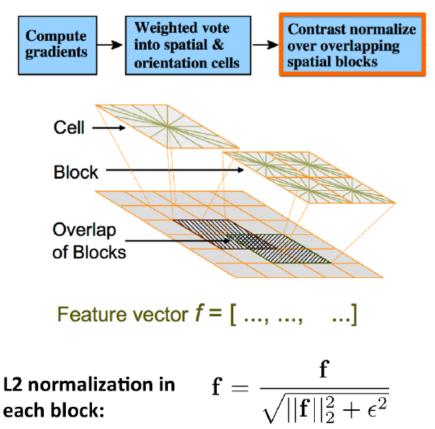


#### • Step 2: Extract Features in Window

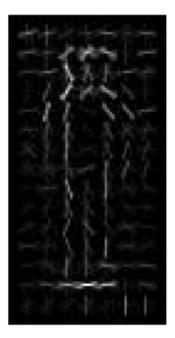
- Histogram of Gradients (HOG) features
- Divide the image into non-overlapping cells (grids) of 8 x 8 pixels
- Compute a histogram of orientations in each cell (similar to SIFT), resulting in a 9-dimensional feature vector.
- We now take blocks, where each has 2 x 2 cells, for HOG normalization.

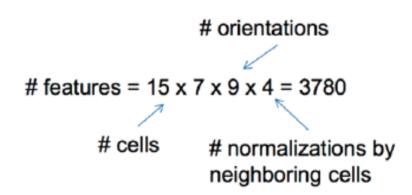


- Step 2: Extract Features in Window
  - Compute a histogram of orientations in each cell (similar to SIFT), resulting in a 9-dimensional feature vector.
  - We now take blocks, where each has 2 x 2 cells, for HOG normalization
  - Normalize each feature vector, such that each block has unit norm. This does not change the dim of the feature, just the magnitude.



- Step 2: Extract Features in Window
  - Normalize each feature vector, such that each block has unit norm. This does not change the dim of the feature, just the magnitude.
  - Each cell is in 4 blocks thus has 4 different normalizations; we make each as a feature representation.
  - For each class of *person*, window is 15 x 7 HOG cells.
  - We vectorize each the feature matrix in each window.





Final descriptor for window (person class in this case)

- Step 3: Detection (classify & accept window if score > threshold)
  - Train a window classifier (e.g., linear or non-linear classifiers)
  - Use the trained classifier to predict presence of object class in each window

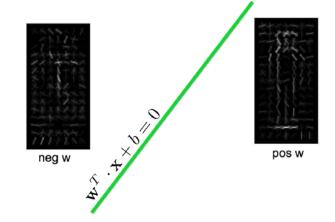


positive training examples



negative training examples

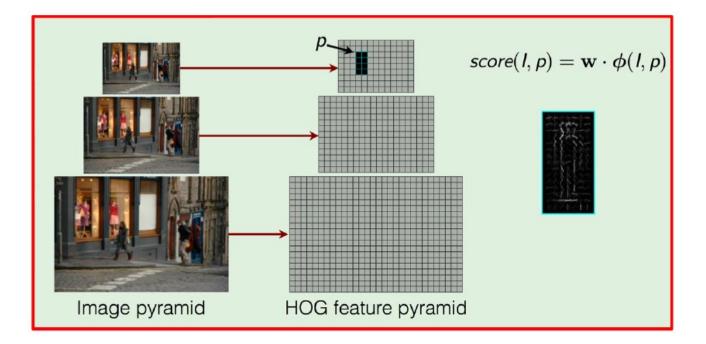




Train classifier. SVM (Support Vector Machines) is typically used.

#### • Step 3: Detection (Classify & accept window if score > threshold)

- Train a window classifier
- Use the trained classifier to predict presence of object class in each window
- During testing, compute the score w<sup>T</sup>x+b in each location, which can be viewed as performing cross-correlation (or convolution) with template w (and add bias b).



#### • Step 4: Cleaning-Up

 Perform a greedy algorithm of non-maxima suppression (NMS) to pick the bounding box with highest score



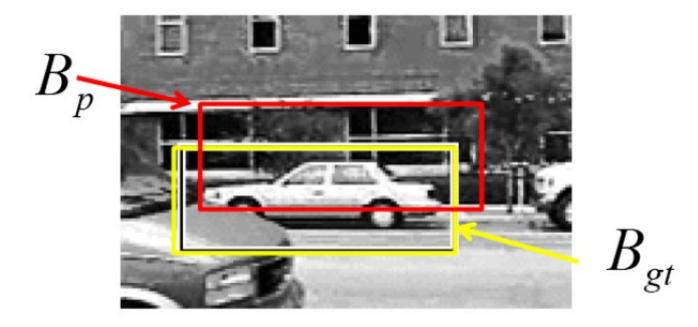
#### Non-maxima suppression (NMS)

$$\text{overlap} = \frac{\operatorname{area}(box_1 \cap box_2)}{\operatorname{area}(box_1 \cup box_2)} > 0.5 \quad \Longrightarrow \quad \boxed{\begin{array}{c} \text{remove} \\ box_2 \end{array}}$$

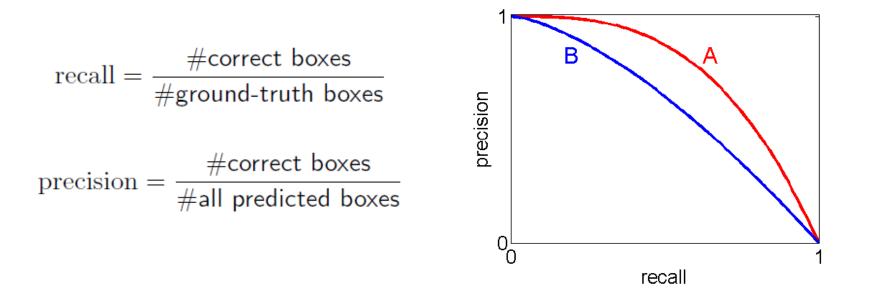
 Remove all boxes that overlap more than XX (typically 50%) with the chosen box

- Evaluation
  - IoU (intersection over union)
    - E.g, detection is correct if IoU between bounding box and ground truth > 50%

$$a_0 = rac{\operatorname{area}(B_p \cap B_{gt})}{\operatorname{area}(B_p \cup B_{gt})}$$

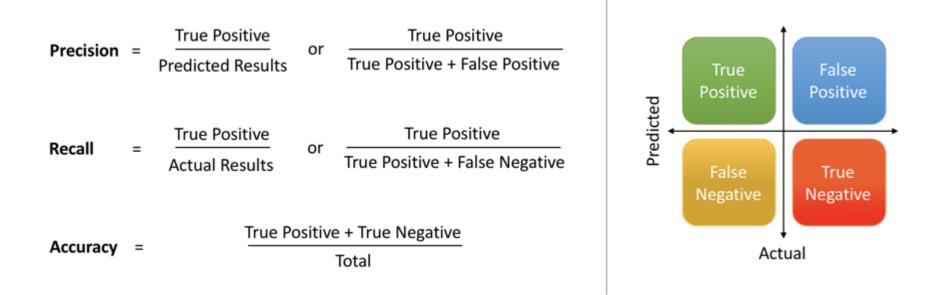


- Evaluation
  - IOU (intersection over union)
    - Mean IOU (mIOU): average IOU across classes
  - Precision and Recall
    - Sort all the predicted boxes according to scores, in a descending order
    - For each location in the sorted list, we compute precision and recall obtained when using top k boxes in the list.

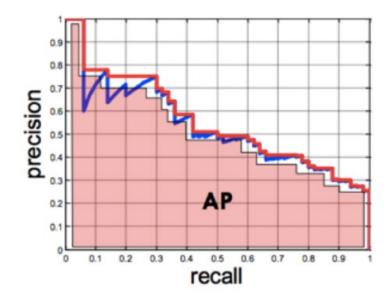


#### • Evaluation

- IOU (intersection over union)
- Precision and Recall



- Evaluation
  - IoU (intersection over union)
  - Precision and Recall
  - Average Precision (AP):
    - Compute the area under P-R curve
    - mean Average Precision (mAP): average of AP across classes

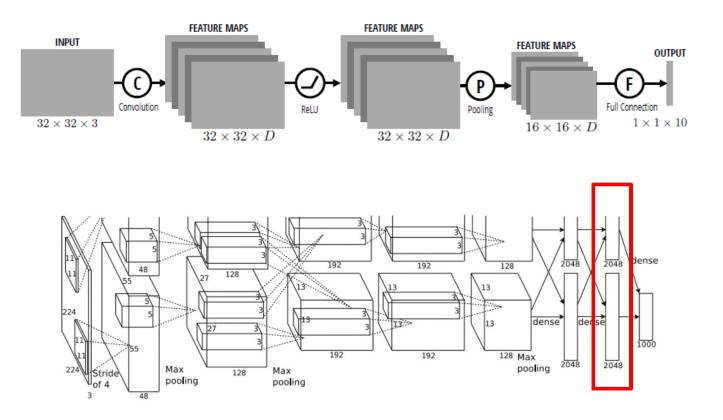


# Something to Think About...

- Sliding window detectors work
  - *very well* for faces
  - *fairly well* for cars and pedestrians
  - *badly* for cats and dogs
- Why are some classes easier than others?

#### **Recall that**

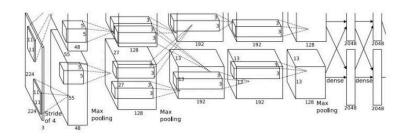
• Visual Features derived by Convolutional Neural Networks





Apply a CNN to many different crops of the image, CNN classifies each crop as object or background

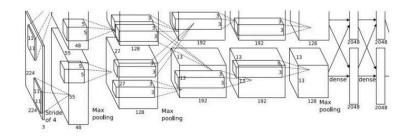




Dog? YES Cat? NO Background? NO

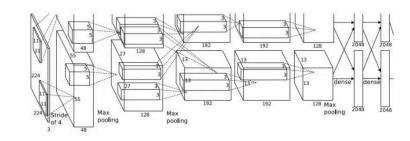


Apply a CNN to many different crops of the image, CNN classifies each crop as object or background



Dog? YES Cat? NO Background? NO

Apply a CNN to many different crops of the image, CNN classifies each crop as object or background



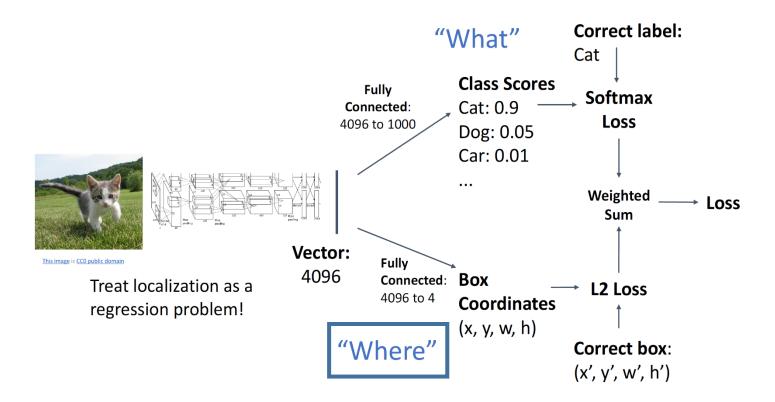
Dog? NO Cat? YES Background? NO



- What could be the problems?
  - Suppose we have an image of 600 x 600 pixels. If sliding window size is 20 x 20, then have (600-20+1) x (600-20+1) = ~330,000 windows to compute.
  - What if more accurate results are needed, need to perform multi-scale detection by
    - Resize image
    - Multi-scale/shape sliding windows
  - For each image, we need to forward pass image regions through CNN for at least ~330,000 times. -> Slow!!!

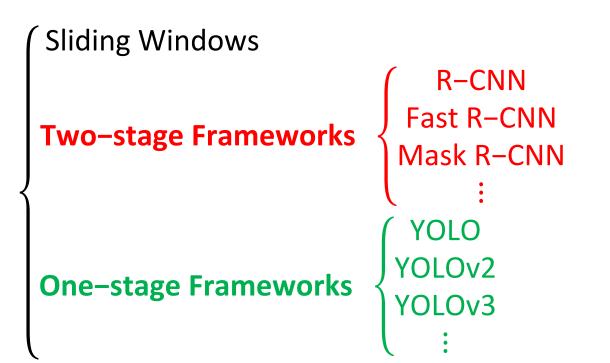
#### **Recap: CNN for Object Detection**

- Need to deal with more than one object
  - How?



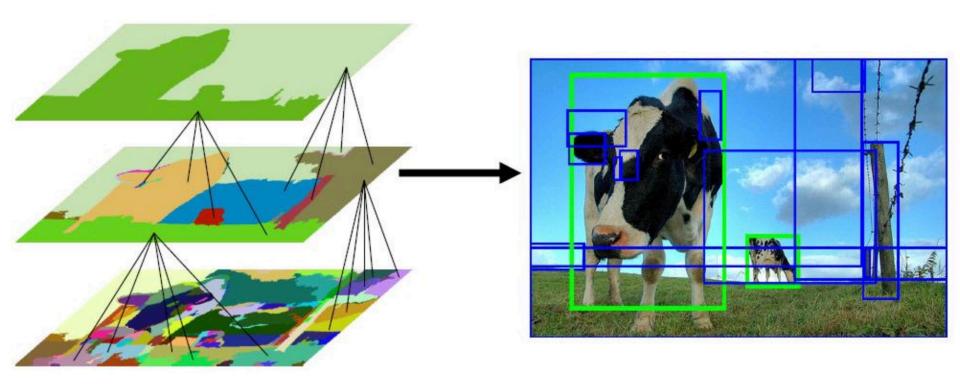
#### **Two-Stage vs. One-Stage Object Detection**

#### Methods

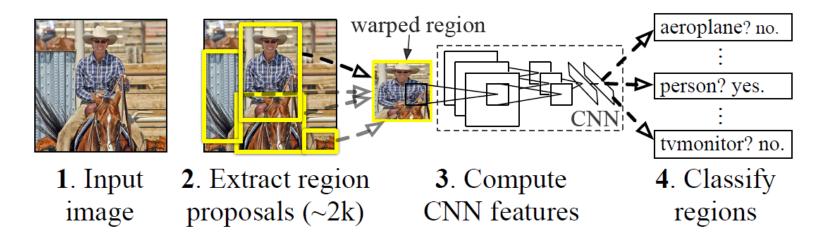


# **Region Proposal**

- Solution
  - Use pre-processing algorithms to filter out some regions first, and feed the regions of interest (i.e., region proposals) into CNN
  - E.g., selective search

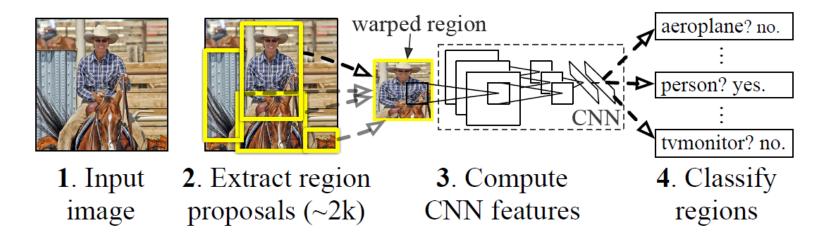


### **R-CNN** (Girshick et al. CVPR 2014)



- Replace sliding windows with "selective search" region proposals (Uijilings et al. IJCV 2013)
- Extract rectangles around regions and resize to 227x227 pixels
- Extract features with fine-tuned CNN (e.g., initialized with network pre-trained on ImageNet)
- Classify last layer of network features with linear classifiers (e.g., SVM/MLP), and refine bounding box localization (bbox regression) simultaneously

### **R-CNN** (Girshick et al. CVPR 2014)



- Ad hoc training objectives:
  - Object class: Fine-tune network with softmax classifier (log loss)
  - Object class: Train post-hoc linear SVMs for each class (hinge loss)
  - Bbox location: Train post-hoc bounding-box regressors (least squares loss)
- Training is extremely slow with lots of disk space.
- Implementation/testing cannot be done in real time.

## **Bounding Box Regression**

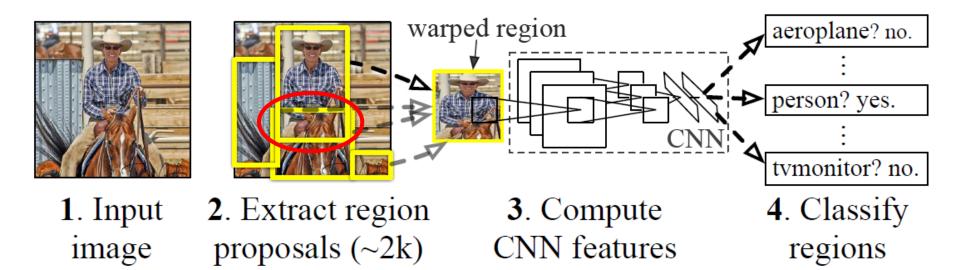
- Intuition
  - If you observe parts of an object, according to the seen examples, you should be able to predict/refine the localization.
    - E.g., given the red bounding box below, since you've seen many airplanes, you know this is not a good localization, you will adjust it to the green one.



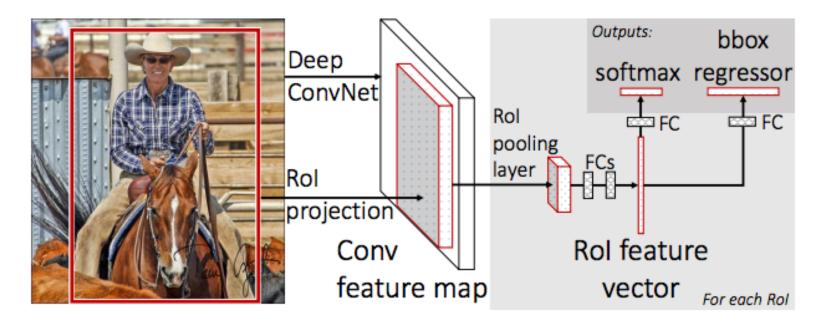


### **R-CNN** (Girshick et al. CVPR 2014)

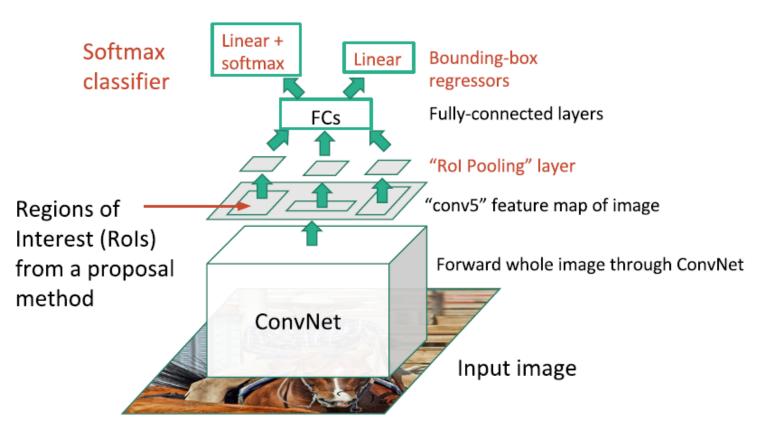
- What could be the problems?
  - Repetitive computation!
     For overlapping regions, we feed it multiple times into CNN



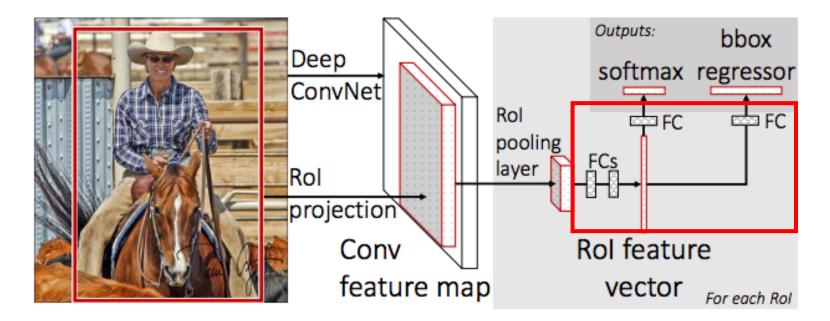
- Solution
  - Why not feed the whole image into CNN only once?
  - Then, crop the feature map instead of the image itself



Solution

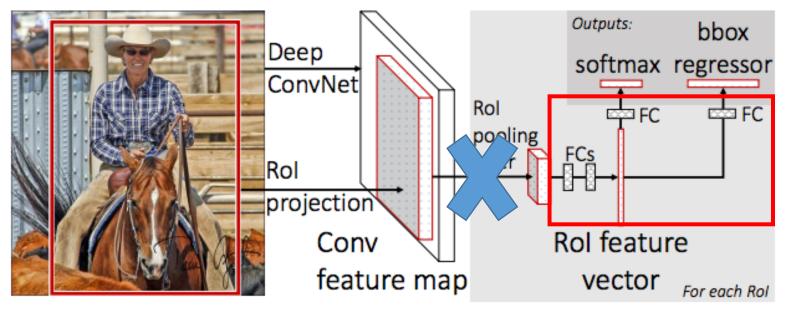


- How to crop features?
  - Since we have fully-connected layers, the size of feature map for each bounding box should be a fixed number



#### • How to crop features?

- Since we have fully-connected layers, the size of feature map for each bounding box should be a fixed number
- Resize/Interpolate the feature map as fixed size?
  - Not optimal. This operation is hard to backprop.
     -> we cannot train the conv layers in CNNs...



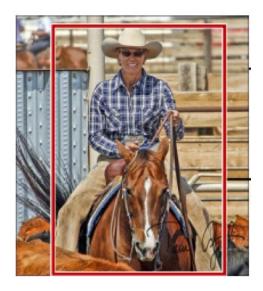
#### • How to crop features?

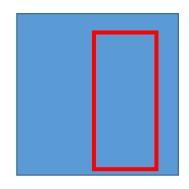
- Since we have fully-connected layers, the size of feature map for each bounding box should be a fixed number
- Resize/Interpolate the feature map as fixed size?
  - Not optimal. This operation is hard to backprop.
    -> we cannot train the conv layers for this problem...
- Rol (Region of Interest) Pooling
  - How?

• Step 1:

Get bounding box for feature map from bounding box for image

• Due to the (down)convolution/pooling operations, feature map would have a smaller size than the original image.



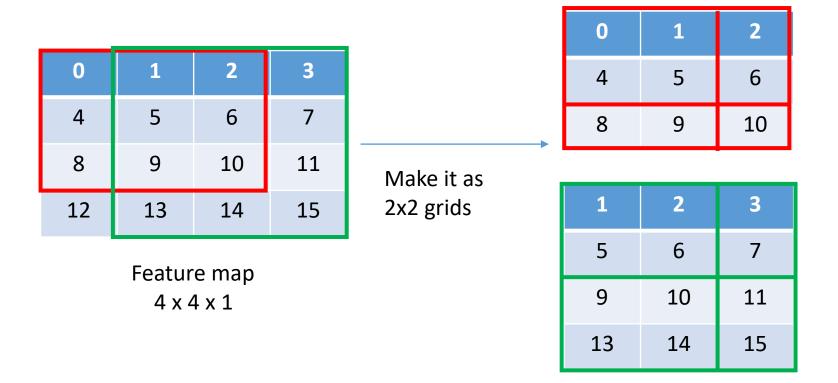


Feature map

• Step 2:

Divide cropped feature map into fixed number of sub-regions

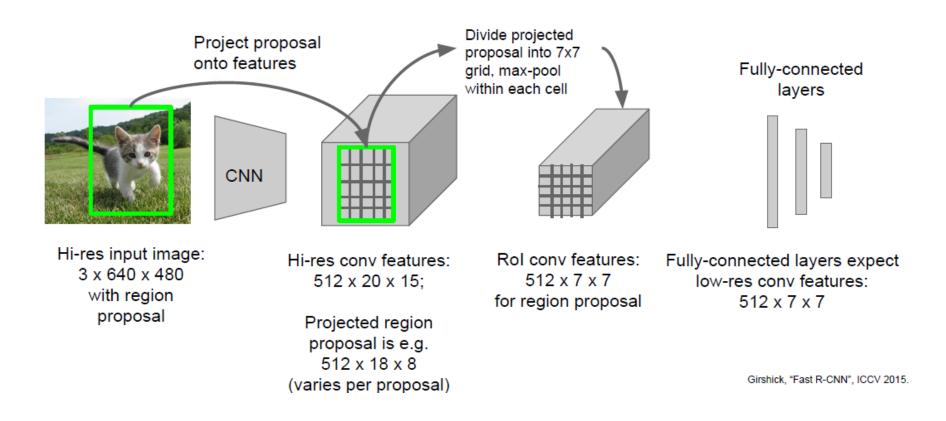
• The last column and last row might be smaller



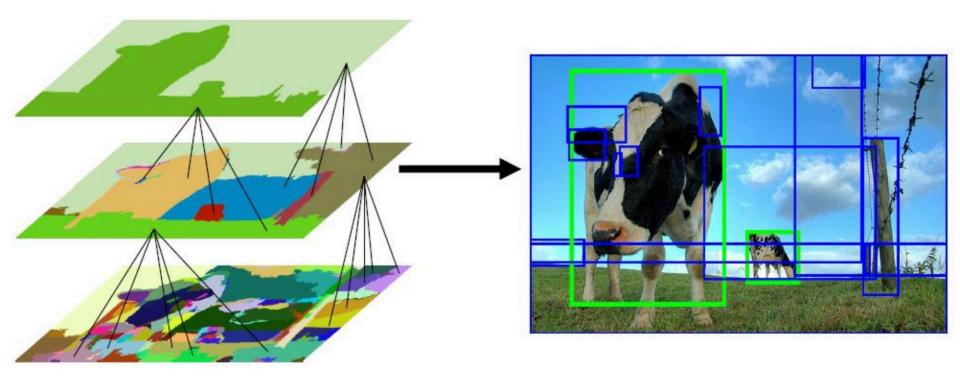
• Step 3:

For each sub-region, perform max pooling (pick the max one)



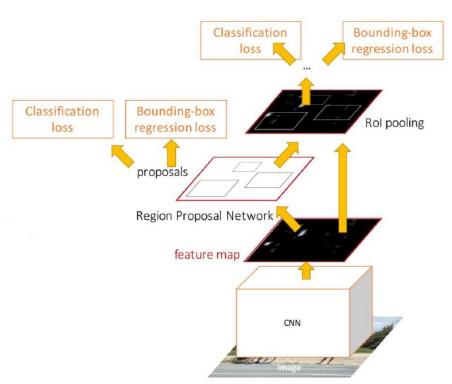


- What could be the problems?
  - We still need to collect the region proposals from a pre-processing step, which does not allow end-to-end learning.



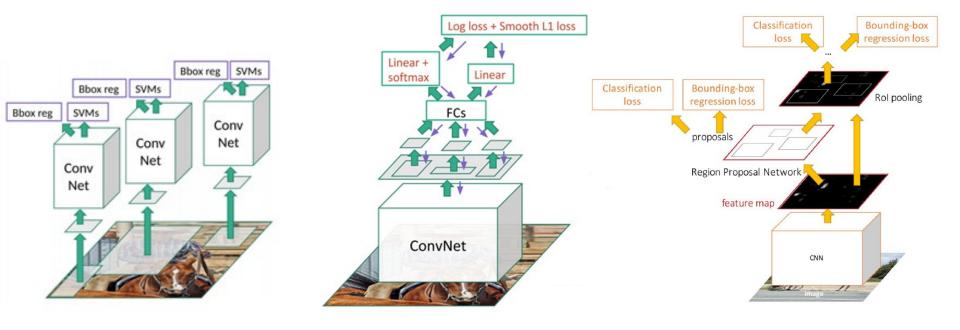
#### Faster R-CNN (Ren et al. NIPS 2015)

- Solution
  - Why not generate region proposals using CNN?
     -> Insert Region Proposal Network (RPN) to predict proposals from features
  - Jointly train with 4 losses:
    - RPN classification loss
    - RPN regress box coordinates
    - Final classification loss
    - Final box coordinates

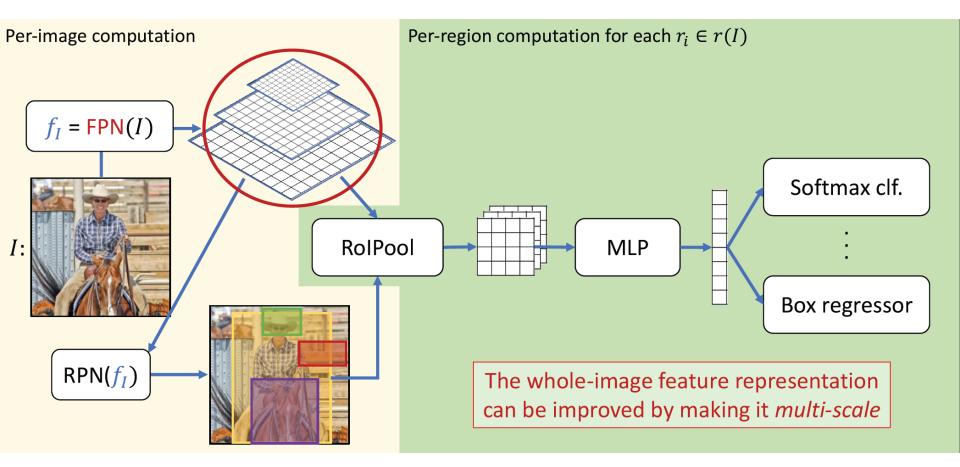


https://arxiv.org/pdf/1506.01497.pdf

#### R-CNN, Fast R-CNN, & Faster R-CNN



### Faster R-CNN with Feature Pyramid Network

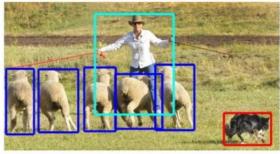


## Faster R-CNN (Ren et al. NIPS 2015)

- What could be the problems
  - Two-stage detection pipeline is still too slow for real-time detection in videos...
  - What about instance-wise information?



(a) Image classification



(b) Object localization



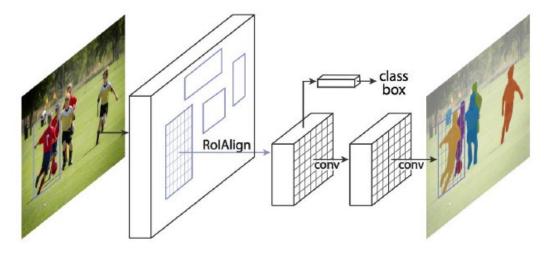
(c) Semantic segmentation

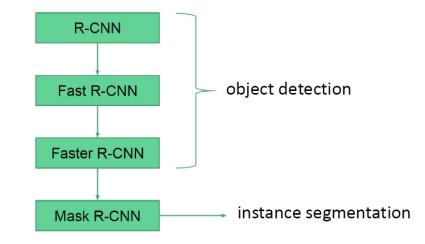


(d) Instance segmentation

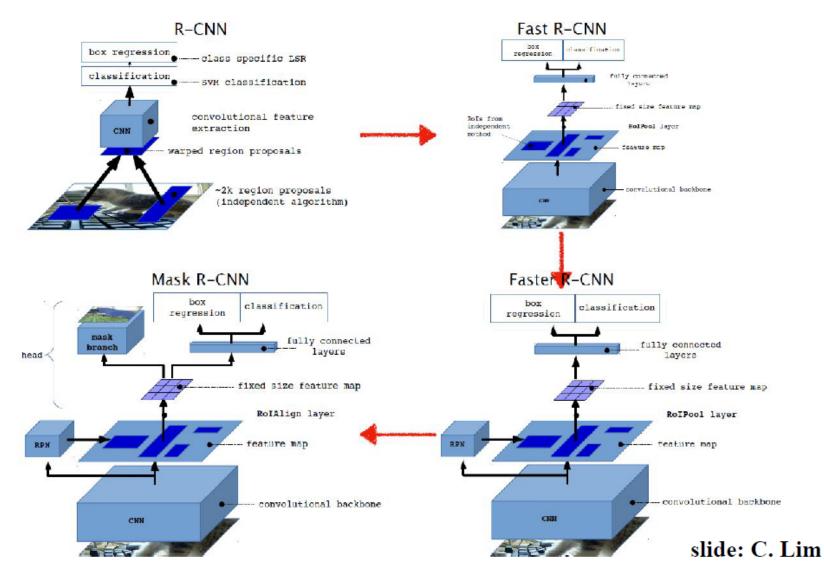
# Mask R-CNN (ICCV2017)

- Goals:
  - Refined detection + precise segmentation
  - Faster R-CNN + FCN
- Overall design:
  - Use of ResNet or feature pyramid net for feature extraction
  - Use RPN to produce proposals (w/ ROI align)
  - Use one detection branch for box classification + regression
  - Use one segmentation branch for box segmentation



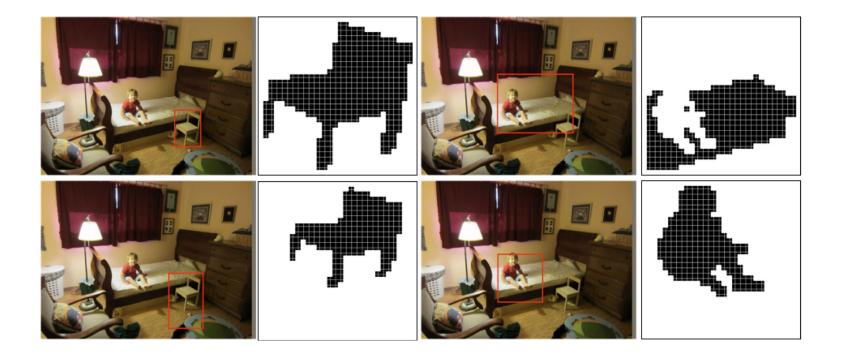


# **R-CNN Family**



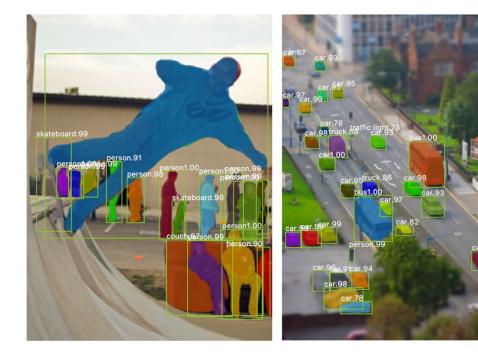
## Mask R-CNN (cont'd)

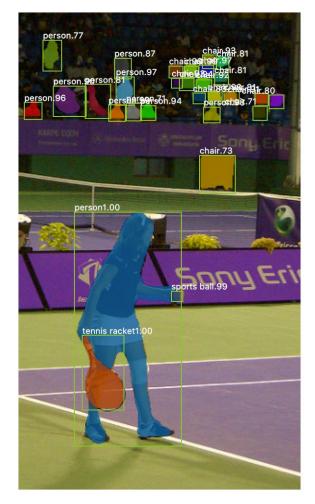
• Example Training Data (requires pixel-level labels)



# Mask R-CNN

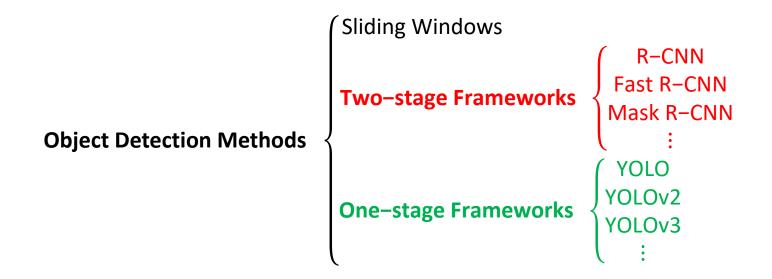
- Very good results!
  - running at 5fps though





# Recap

- So far, the introduced methods follow a **two-stage** framework.
  - 1. Region Proposal
  - 2. Per-Region Classification/Regression
- Can we make it faster by integrating the above two steps into one single network?



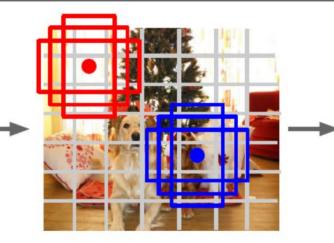
# **One-Stage Object Detection: Detection without Proposals**

Go from input image to tensor of scores with one big convolutional network!



Input image 3 x H x W

Redmon et al, "You Only Look Once: Unified, Real-Time Object Detection", CVPR 2016 Liu et al, "SSD: Single-Shot MultiBox Detector", ECCV 2016



Divide image into grid 7 x 7

Image a set of **base boxes** centered at each grid cell Here B = 3 Within each grid cell:

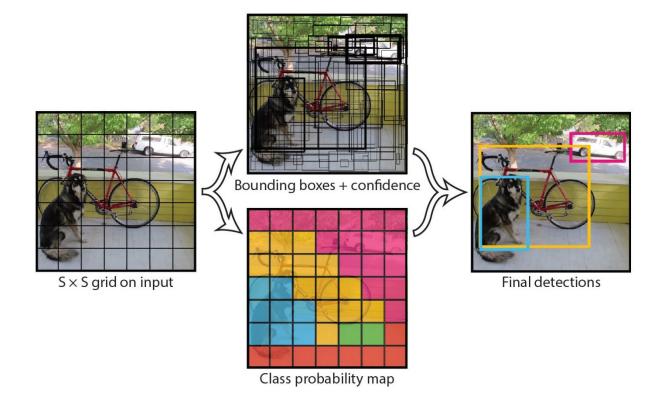
- Regress from each of the B base boxes to a final box with 5 numbers:
  - (dx, dy, dh, dw, confidence)
- Predict scores for each of C classes (including background as a class)

Output:  $7 \times 7 \times (5 * B + C)$ 

# You Only Look Once (YOLO)

Divide the image into an  $S \times S$  grid and for each grid cell predicts B bounding boxes, confidence for those boxes, and C class probabilities.

These predictions are encoded as an  $S \times S \times (B * 5 + C)$  tensor.



## You Only Look Once (YOLO)

class confidence score = box confidence score × conditional class probability

box confidence score  $\equiv P_r(object) \cdot IoU$ conditional class probability  $\equiv P_r(clas_{S_i}|object)$ class confidence score  $\equiv P_r(clas_{S_i}) \cdot IoU$ 

= box confidence score  $\times$  conditional class probability

#### where

 $P_r(object)$  is the probability the box contains an object. IoU is the IoU (intersection over union) between the predicted box and the ground truth.  $P_r(class_i|object)$  is the probability the object belongs to  $class_i$  given an object is presence.  $P_r(class_i)$  is the probability the object belongs to  $class_i$ 

# You Only Look Once (YOLO)

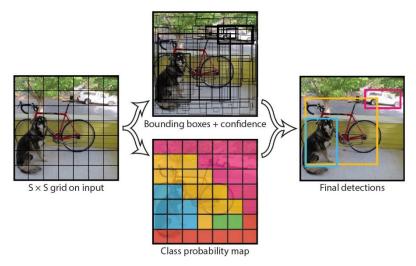
• **Fast**. Good for real-time processing.

#### • End-to-end learnable.

Predictions (object locations and classes) are made from one single network.

- Access to the entire image. Region proposal methods limit the classifier to the specific region. YOLO accesses to the whole image in predicting boundaries. With additional context, result in fewer false positives in background areas.
- Spatial diversity.

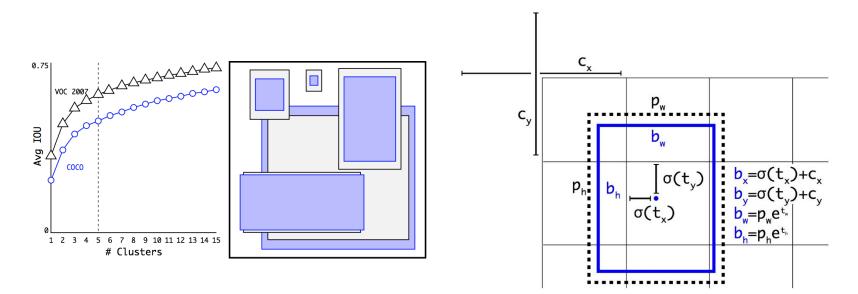
Detect one object per grid cell. It enforces spatial diversity in making predictions.



## YOLOv2

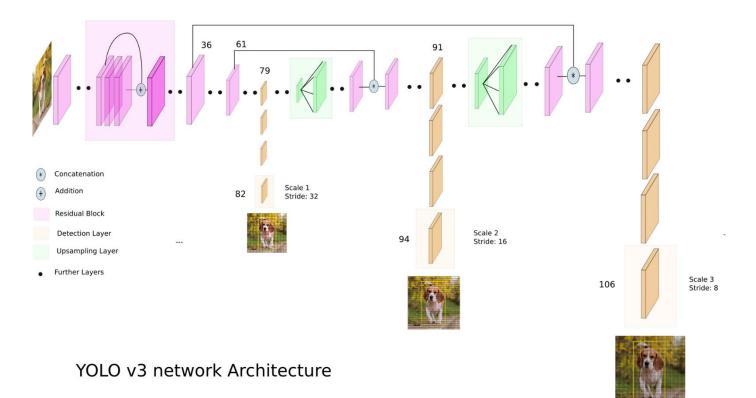
- Predetermined bounding box shape (anchor boxes)
   Guesses that are common for real-life objects using k-means clustering
   ⇒ Predicts offsets rather than bounding boxes themselves
- Move the class prediction from the cell level to the boundary box level Each *bounding box* (instead of each *cell*) produces a class prediction

$$S \times S \times (B * 5 + C) \Longrightarrow S \times S \times (B * (5 + C))$$



## YOLOv3

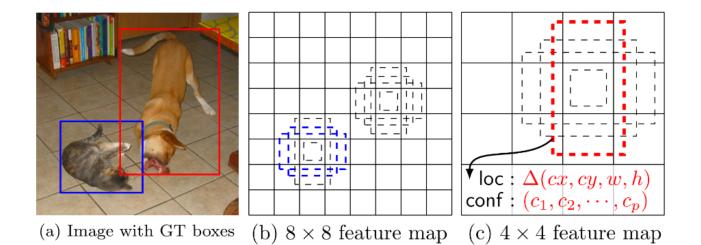
Feature Pyramid Networks (FPN) like Feature Pyramid
 YOLOv3 makes predictions at 3 different scales (similar to the FPN).



 $S \times S \times (3 * (5 + C))$ 

## Single Shot MultiBox Detector (SSD)

Propose multiple default boxes per grid at different scales



# Recap

### **Object Detection Methods**

Sliding Windows

**Two-stage Frameworks** 

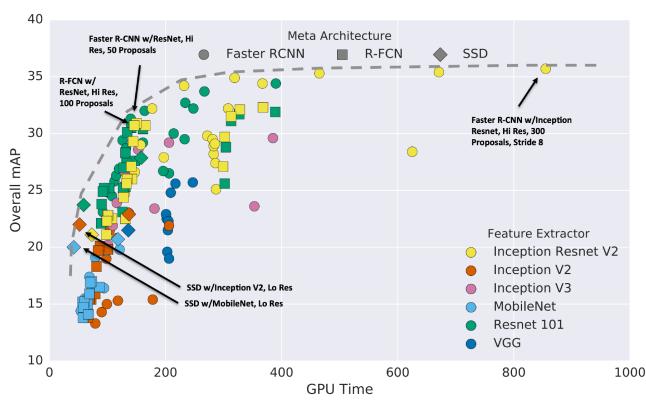
(High Accuracy, Slow)

**One-stage Frameworks** 

(Good Accuracy, Very Fast)

R-CNN Fast R-CNN Mask R-CNN : YOLO YOLOv2 YOLOv3 :

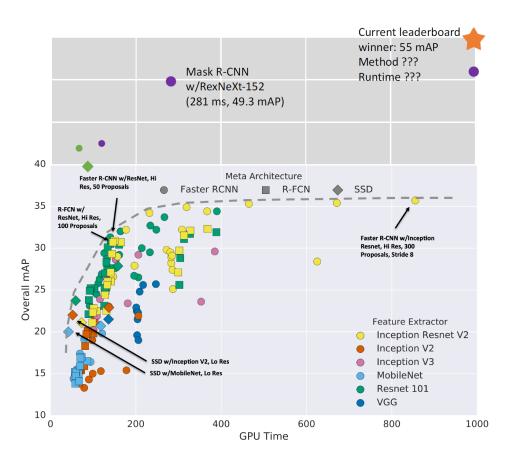
## Remarks



#### Takeaways:

- Two stage method (Faster R-CNN) get the best accuracy, but are slower
- Single-stage methods (SSD) are much faster, but don't perform as well
- Bigger backbones improve performance, but are slower

## Remarks (cont'd)

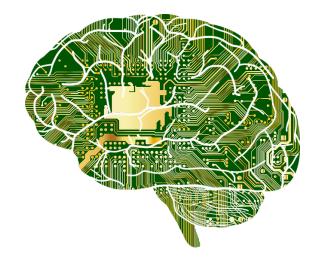


These results are a few years old ... since then GPUs have gotten faster, and we've improved performance with many tricks:

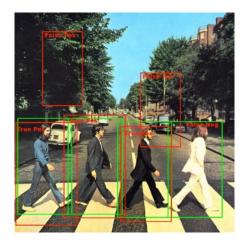
- Train longer!
- Multiscale backbone: Feature Pyramid Networks
- Better backbone: ResNeXt
- Single-Stage methods have improved
- Very big models work better
- Test-time augmentation pushes numbers up
- Big ensembles, more data, etc

### What's to Be Covered Today...

- Segmentation
- Object Detection
- Generative Model
  - Autoencoder (AE)
  - Variational Autoencoder (VAE) (next week)

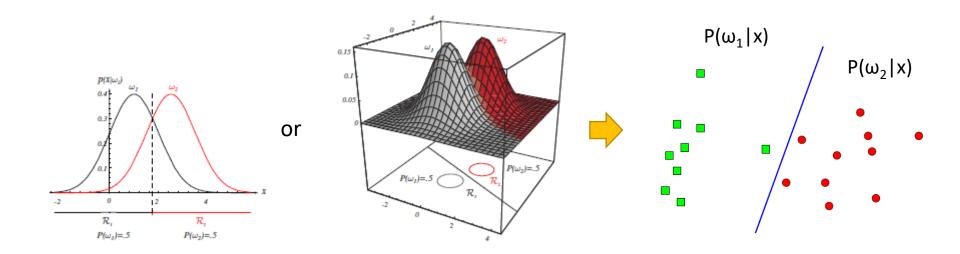




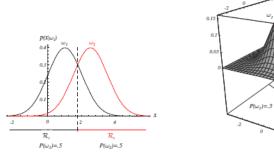


# **Discriminative vs. Generative Models**

- Discriminative Models
  - Model posteriors  $P(\omega|x)$  from likelihoods  $P(x|\omega)$ where x is the input data, and  $\omega$  indicates the class of interest
  - Example (posterior)



- Generative Models
  - Model likelihoods  $P(x|\omega)$  with priors  $P(\omega)$  (i.e., modeling  $P(x|\omega) P(\omega)$ ) where x is the input data, and  $\omega$  indicates the class of interest

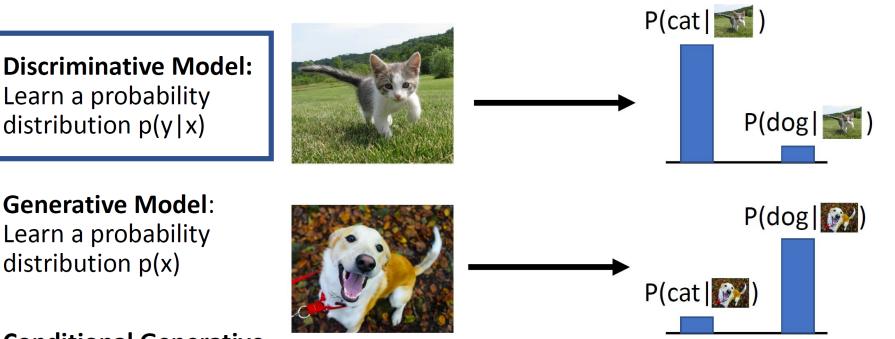


• Example

(CelebA)

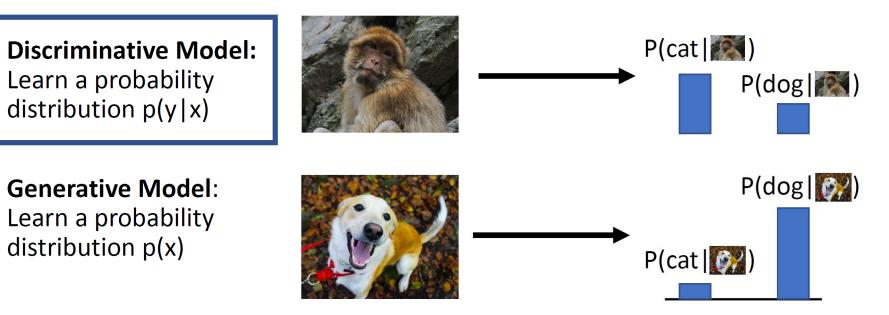


Sample Generator (Karras et al, 2017)



**Conditional Generative Model:** Learn p(x|y)

Discriminative model: the possible labels for each input "compete" for probability mass. But no competition between **images** 



**Conditional Generative Model:** Learn p(x|y)

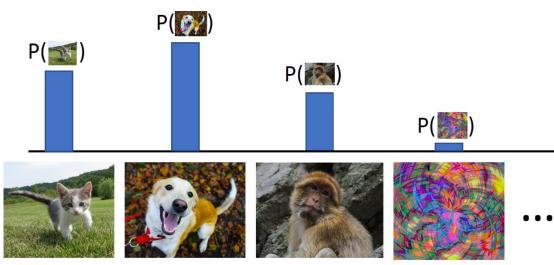
Discriminative model: No way for the model to handle <u>unreasonable inputs</u>; it must give label distributions for all images

#### **Discriminative Model:**

Learn a probability distribution p(y|x)

**Generative Model**: Learn a probability distribution p(x)

**Conditional Generative Model:** Learn p(x|y)



Generative model: All possible images compete with each other for probability mass

Model can "reject" unreasonable inputs by assigning them small values

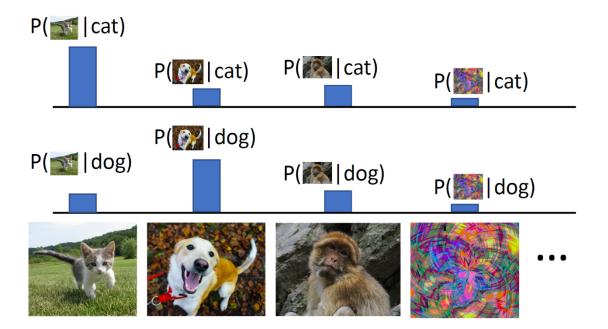
**Discriminative Model:** 

Learn a probability distribution p(y|x)

Generative Model:

Learn a probability distribution p(x)

**Conditional Generative Model:** Learn p(x|y)



Conditional Generative Model: Each possible label induces a competition among all images

#### **Discriminative Model:**

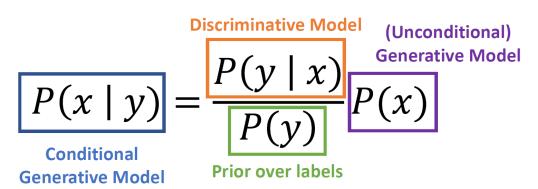
Learn a probability distribution p(y|x)

#### Generative Model:

Learn a probability distribution p(x)

**Conditional Generative Model:** Learn p(x|y)

### Recall Bayes' Rule:



We can build a conditional generative model from other components!

### **Additional Remarks**

- Discriminative Models
  - Learn a (posterior)probability distribution p(y|x)
  - Assign labels to each instance x
  - Supervised learning
- Generative Models
  - Learn a probability distribution p(x)
  - Data representation, detect outliers, etc.
  - Unsupervised learning

### What Have Been Done Using Deep Generative Models?

• 5+ years of progress on synthesizing face images



## What Have Been Done Using Deep Generative Models?

• 2 years of progress on synthesizing images (ImageNet)

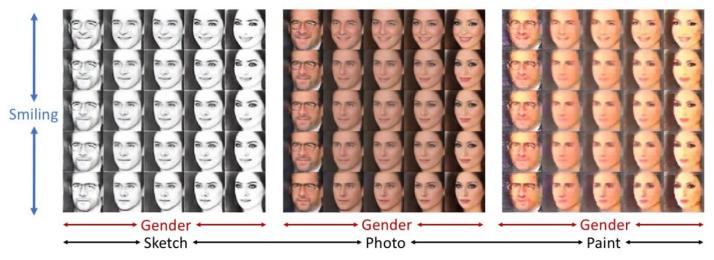


### (Odena 2018)

Slide credit: I. Goodfellow

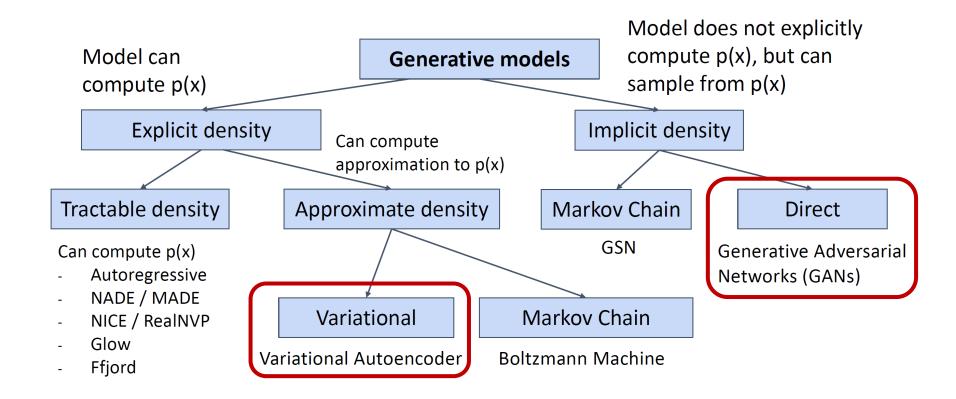
# Why We Need Generative Models?

- Remarks
  - Able to process data information (e.g., priors like attribute, category, etc.) for synthesis, prediction, or recognition purposes
    - For example, with latent feature z derived from x, one may have P(z) may describe image variants.
    - Or, z in P(z) may annotate object categorical or attribute information.



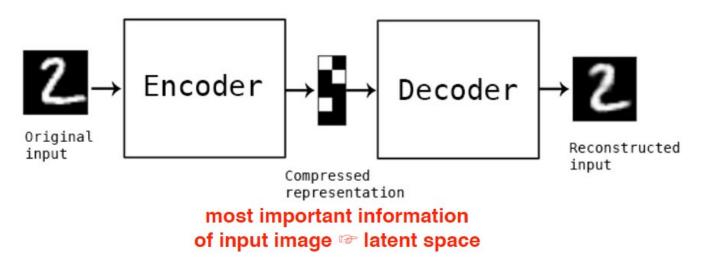
• We will talk about a variety of visual applications based on generative models

### **Taxonomy of Generative Models**



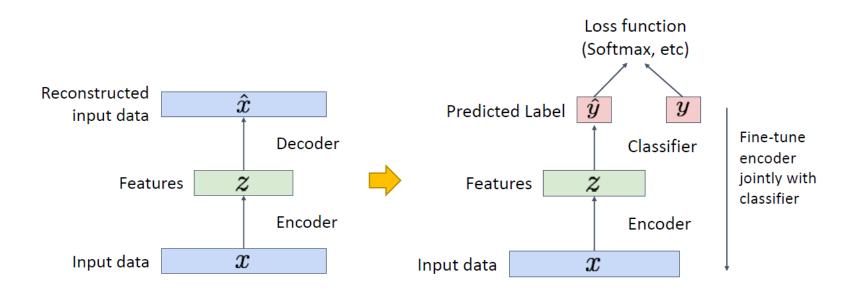
### Take a Deep Look to Discover Latent Variables/Representations

- Autoencoder
  - Autoencoding = encoding itself with recovery purposes
  - In other words, encode/decode data with reconstruction guarantees
  - Latent variables/features as deep representations
  - Example objective/loss function at output:
    - L2 norm between input and output, i.e.,



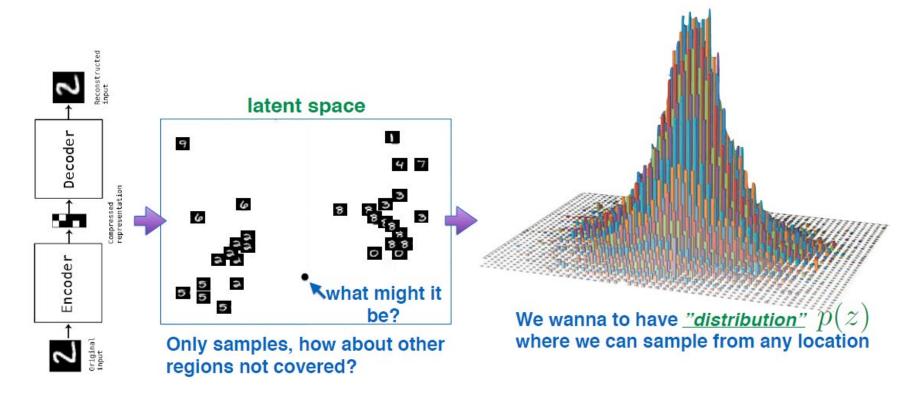
### Take a Deep Look to Discover Latent Variables/Representations (cont'd)

- Autoencoder (AE) for downstream tasks
  - Train AE with reconstruction guarantees
  - Keep encoder (and the derived features) for downstream tasks (e.g., classification)
  - Thus, a trained encoder can be applied to initialize a supervised model

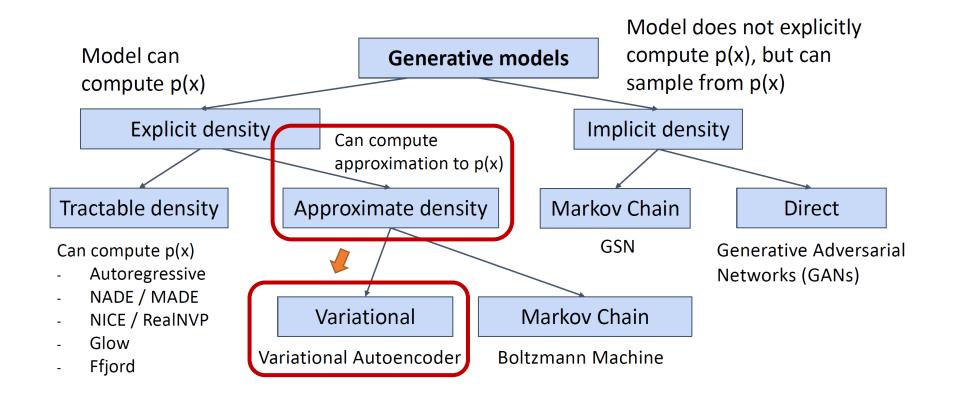


### Take a Deep Look to Discover Latent Variables/Representations (cont'd)

• What's the Limitation of Autoencoder?

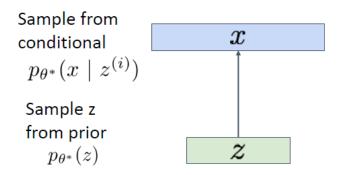


### **Taxonomy of Generative Models**



### **Variational Autoencoder**

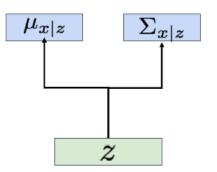
- Probabilistic Spin on AE
  - Learn latent feature z from raw data x
  - Sample from the latent space (via model) to generate data



Assume simple prior p(z), e.g. Gaussian

Represent p(x|z) with a neural network (Similar to **decoder** from autencoder)

p(x|z) is implemented via a (probabilistic) decoder



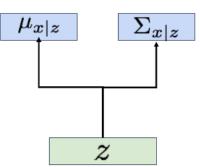
Decoder inputs z, outputs mean  $\mu_{x|z}$ and (diagonal) covariance  $\sum_{x|z}$ 

Sample x from Gaussian with mean  $\mu_{x|z}$  and (diagonal) covariance  $\sum_{x|z}$ 

### Variational Autoencoder (cont'd)

- Remarks
  - Train VAE via maximum likelihood of data
  - Note that we don't observe z & need to marginalize it:

$$p_{\theta}(x) = \int p_{\theta}(x, z) dz = \int p_{\theta}(x|z) p_{\theta}(z) dz$$



- We can compute with the decoder module, and we assume Gaussian prior for z, i.e.,
- However, can't integrate over all possible z!
- Recall that we have Bayes' rule:

$$p_{\theta}(x) = \frac{p_{\theta}(x \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x)}$$

We can't compute  $p_{\theta}(z \mid x)$ , but we can train the encoder module to learn

$$q_{\phi}(z \mid x) \approx p_{\theta}(z \mid x)$$

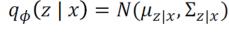
### Variational Autoencoder (cont'd)

Now we have...

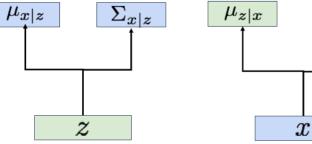
latent code z, gives distribution over data x

Decoder network inputs Encoder network inputs data x, gives distribution over latent codes z

$$p_{\theta}(x \mid z) = N(\mu_{x \mid z}, \Sigma_{x \mid z})$$



 $\Sigma_{z|x|}$ 



• If we ensure  $q_{\phi}(z \mid x) \approx p_{\theta}(z \mid x)$ then we have  $p_{\theta}(x) \approx \frac{p_{\theta}(x \mid z)p(z)}{q_{\phi}(z \mid x)}$ 

$$= E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}(q_{\phi}(z|x), p(z)) + D_{KL}(q_{\phi}(z|x), p_{\theta}(z|x))$$

Data reconstruction

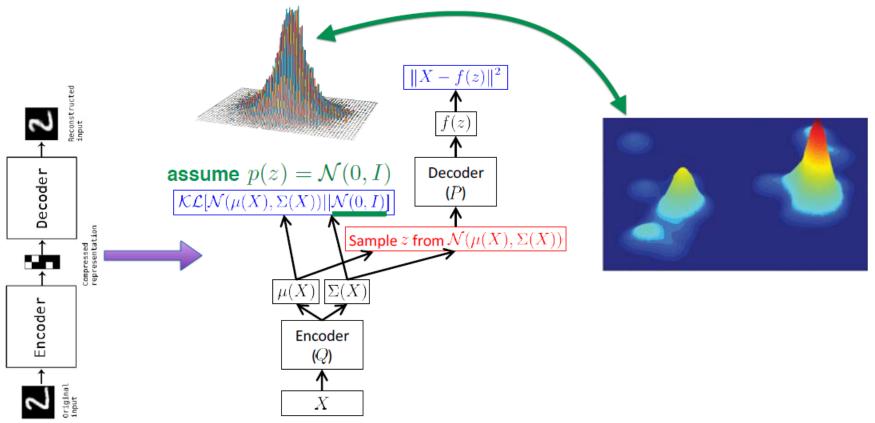
KL divergence between sample distribution from the encoder and the prior KL divergence between sample distribution from the encoder and the posterior of data

$$\Rightarrow \log p_{\theta}(x) \ge E_{z \sim q_{\phi}(z|x)}[\log p_{\theta}(x|z)] - D_{KL}\left(q_{\phi}(z|x), p(z)\right)$$

i.e., variational lower bound on the data likelihood  $p_{\scriptscriptstyle \Theta}(x)$ 

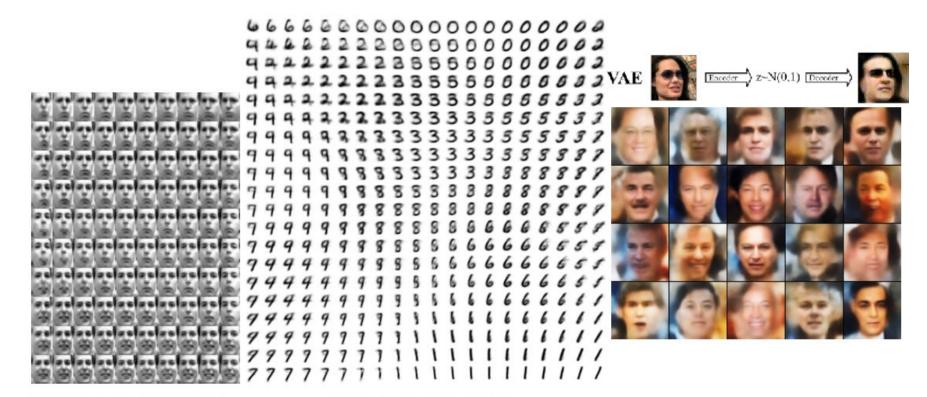
### Summary: From Autoencoder to Variational Autoencoder

Now is a "distribution", we can assume it to be a distribution easy to sample from, e.g. Gaussian



### From Autoencoder to Variational Autoencoder (cont'd)

• Example Results

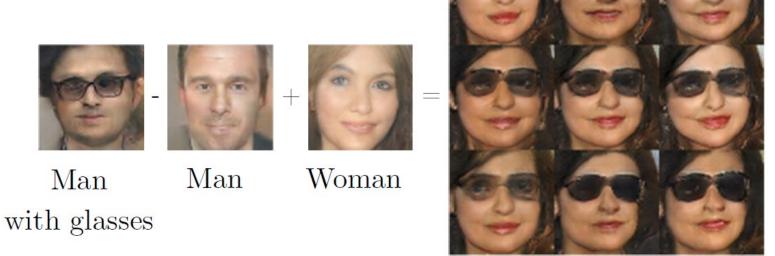


(a) Learned Frey Face manifold

(b) Learned MNIST manifold

### From Autoencoder to Variational Autoencoder (cont'd)

- Example Results
  - A' A + B = B'



Woman with Glasses

### What We've Covered Today...

- Segmentation
- Object Detection
- Generative Model
- Next time: GAN & Diffusion Models
- HW #1 is out & due Oct. 10<sup>th</sup> Mon 23:59



